

Second test in Macro-econometrics

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1. Facts about integration and cointegration.[11 points]

- (a) What is a first-order integrated (I(1)) variable?
- (b) Try and provide an example for a non-stationary process/variable that is *not* I(1).
- (c) When are two time-series variables said to be cointegrated?
- (d) What do econometricians mean when they talk about the ‘super-consistency’ of the estimator in a cointegrating regression?

2. An error-correction system. [12 points] The dynamic behavior of two macroeconomic aggregates X and Y follows a VAR(1) model

$$\begin{bmatrix} X_t \\ Y_t \end{bmatrix} = \begin{bmatrix} 1.1 & -0.2 \\ -0.2 & 1.4 \end{bmatrix} \begin{bmatrix} X_{t-1} \\ Y_{t-1} \end{bmatrix} + \begin{bmatrix} \varepsilon_{1t} \\ \varepsilon_{2t} \end{bmatrix}.$$

- (a) Write the model in the error-correction form $\Delta x_t = \mathbf{\Pi}x_{t-1} + \varepsilon_t$ for $x = (X, Y)'$, and particularly determine the matrix $\mathbf{\Pi}$. This impact matrix should have a rank of 1. Can you confirm this?
- (b) Try and find a factorization of $\mathbf{\Pi} = \alpha\beta'$. Provide the cointegrating vector β . [Hint: we assume that explosive roots and unit roots other than one are not present in this system.]
- (c) We find another macroeconomic variable Z that follows the AR(1) model $Z_t = 0.5Z_{t-1} + \varepsilon_t$. Provide the characteristic polynomial and its root (zero) to show that this variable is stable.
- (d) Now suppose we are joining all three variables into a big system

$$\begin{bmatrix} X_t \\ Y_t \\ Z_t \end{bmatrix} = \begin{bmatrix} 1.1 & -0.2 & 0 \\ -0.2 & 1.4 & 0 \\ 0 & 0 & 0.5 \end{bmatrix} \begin{bmatrix} X_{t-1} \\ Y_{t-1} \\ Z_{t-1} \end{bmatrix} + \begin{bmatrix} \varepsilon_{1t} \\ \varepsilon_{2t} \\ \varepsilon_{3t} \end{bmatrix}.$$

Try to re-write it in its error-correction form. What is the rank of the impact matrix $\mathbf{\Pi}$ now?

3. Panels [12 points] Someone wishes to estimate classical Phillips curves in a panel of 19 eurozone countries for annual data 2000-2015. [Some of these countries joined the eurozone later, as we know, but we do not take this issue into account.] The available variables are a rate of CPI inflation π_{it} and an unemployment rate u_{it} . Two classical functions are targeted, the static model

$$\pi_{it} = \beta_0 + \beta_1 u_{it} + \varepsilon_{it}$$

and the dynamic Phillips curve

$$\pi_{it} = \beta_0 + \beta_1 \pi_{i,t-1} + \beta_2 u_{it} + \varepsilon_{it},$$

in both cases assuming the errors consisting of a country *effect* and an idiosyncratic error, i.e. $\varepsilon_{it} = \alpha_i + v_{it}$.

- (a) *A priori*, would you choose a fixed-effects or a random-effects approach here? Why?
- (b) It turns out that a Hausman test rejects for the static model. Which model/estimator does this suggest?
- (c) What is the problem if you use the same estimator for the dynamic version? What can you do to resolve this problem?
- (d) Try and provide an economic interpretation of the effects α_i in this application.