Heat-Diffusion Central Peak in the Elastic Susceptibility of KSCN

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We present the first low frequency (0.1–20 Hz) measurements of the complex elastic constant on KSCN single crystals. Our measurements show very slow sample-size dependent elastic relaxations, at temperatures ranging from $T_c = 415$ K up to the order-disorder phase transition temperature $T_c$. The data can be well explained with the assumption of temperature or equivalent entropy fluctuations. This phenomenon, although intimately related to the thermal-diffusion central peak phenomenon is, to our knowledge, for the first time seen in a macroscopic elastic susceptibility.

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Potassium thiocyanate (KSCN) is a model crystal for studying order-disorder phase transitions [1]. A first order phase transition at $T_c = 415$ K leads the crystal from a disordered tetragonal ($D_{4h}$) high temperature phase to an ordered antiferrodistortive orthorhombic ($D_{2h}$) low temperature phase [2]. Distinct precursor effects preface this phase transition in both phases. From neutron scattering it was found that in the low temperature phase the precursor clusters appear already 40 K below $T_c$ [3]. They consist of small dynamic domains which are in an antiphase relation with the long range ordered matrix of the crystal [3]. The average cluster size $\xi^- \approx 20$ Å depends weakly on temperature and their lifetime $\tau_q^- > 10^{-11}$ s. At $T_c$ the long range order parameter $\eta$ vanishes, but short range order persists up to the melting point, i.e., $T_c + 30$ K [3]. NMR measurements have shown that these short range ordered clusters consist of dynamic orthorhombic microdomains with a lifetime $10^{-5} < \tau_q^+ < 10^{-2}$ s [4]. According to diffuse neutron scattering the correlation length $\xi^+ \approx 35$ Å at $T_c + 2$ K and decreases with increasing temperature [3].

To obtain additional insight into the dynamics of the phase transition we performed detailed low frequency ($f = 0.1–20$ Hz) three-point bending measurements of the complex elastic constant in KSCN. We found a very distinct, probe geometry dependent relaxation process at very low frequencies. For example, for a sample with thickness $h = 0.6$ mm the relaxation time is $\tau_{th} \approx 10^{-1}$ s. By varying the thickness $h$ of the sample the relation $\tau_{th} = (\pi^2 D)^{-1} h^2$ is obtained yielding $D = 2.8 \times 10^{-3}$ cm$^2$ s$^{-1}$. Since this value of $D$ is typical for the thermal diffusivity constants of similar crystals we attribute the observed low frequency dispersion of the elastic susceptibility to a crossover from the isothermal limit ($\omega \tau_{th} \ll 1$) to the adiabatic limit ($\omega \tau_{th} \gg 1$) which occurs because of the effect of temperature (entropy) fluctuations. This effect is closely related to the heat-diffusion “central peak” phenomenon, a subject which was intensively studied in the 1970s by neutron scattering [5] and light scattering [6–9] experiments.

In 1977, Lines and Glass [10] predicted the existence of an ultralow-frequency dispersion due to entropy fluctua-

![FIG. 1. Three-point bending geometry.](image-url)
FIG. 2. Measured temperature dependences of the real ($C_{33}^{\text{eff}}$) and the imaginary ($C_{33}^{\text{eff}}$) part of the complex elastic constant for frequencies of 0.2 and 2 Hz. (▲) adiabatic and (●) isothermal elastic constants are obtained from the frequency scans at various temperatures (Fig. 3). The measurements at $10^7$ Hz (■) were previously performed with ultrasonic technique [14].

(ultrasonic measurement [14]). In addition, the adiabatic and isothermal values extrapolated from frequency scans (Fig. 3) performed at various temperatures are shown. At low frequencies $C_{33}^{\text{eff}}$ exhibits a large negative anomaly at $T_c$. The magnitude of the jump decreases with increasing measurement frequency and is reduced by a factor of about 2 for the adiabatic elastic constant. At ultrasonic frequencies ($10^7$ Hz) the negative dip vanished completely [14].

Simultaneously with the onset of the dip in $C_{33}^{\text{eff}}$, the imaginary part $C_{33}^{\text{eff}}$ of the complex elastic constant increases with increasing temperature, displaying a maximum at $T_c$. With further heating $C_{33}^{\text{eff}}$ falls to zero slightly above $T_c$. For $n = 0.6$ mm the strongest damping is observed around 1 Hz. To get further information on the dynamics we performed frequency scans for $C_{33}^{\text{eff}}$ and $C_{33}^{\text{eff}}$ at various temperatures (Fig. 3). The curves are characteristic for a relaxation process with a rather long, slightly temperature dependent relaxation time $\tau_1 \approx 0.1$ s. The connection between the 20 Hz region and the 10 MHz region requires a second relaxation process with $10^{-7} < \tau_2 < 10^{-3}$ s.

In the following we will analyze the data in the frame of a thermal diffusion central peak model [7]. The details of the calculations will be published elsewhere [15]. The theory is based on the following Landau-Ginzburg expansion of the free energy density [1]

$$F = F_0 + \frac{A}{2} (T - T_0) \eta^2 + \frac{B}{4} \eta^4 + \frac{C_{33}^{\text{eff}}}{6} \eta^6 + \frac{1}{2} g(\nabla \eta)^2 + \frac{\alpha}{2} \eta^2 \epsilon_3 + \frac{C_{33}^{\text{eff}}}{2} \epsilon_3^2 - \sigma_3 \epsilon_3,$$

where $\eta$ is the primary order parameter describing the orientational ordering of the SCN$^-$ molecules with the critical wave vector $Q_c = a^*/2$ [16]. $\epsilon_3$ is the longitudinal strain in Voigt notation and $C_{33}^{\text{eff}}$ is the corresponding bare elastic constant. $\sigma_3$ denotes the stress in $z$ direction.

In the presence of $\eta^2 \epsilon$ coupling in (1) the elastic anomaly can be written (neglecting three- and four-point correlations of order parameter fluctuations) as [17]

$$C_{33}^{\text{eff}}(Q, \omega) = C_{33}^{\text{K}} - \alpha^2 \eta_0^2(Q_c) \chi_\eta(q - Q_c, \omega),$$

where $\eta_0(Q_c)$ is the equilibrium order parameter. In the presence of a central peak mechanism the order parameter susceptibility $\chi_\eta$ has the following form [7]:

$$\chi_\eta^{-1}(q - Q_c, \omega) = \chi_\eta^{-1,K}(q - Q_c, 0) \times \left[1 - i\omega \tau_\eta(q - Q_c)\right] - \frac{\delta^2 i\omega / \gamma}{1 - i\omega / \gamma}.$$

The first part in (3) is the so-called Landau-Khalatnikov term which is obtained from a relaxational
behavior of the order parameter fluctuations, i.e.,
\[ \delta \eta (q, t) = \delta \eta (q, 0) e^{-i/t_{\tau}(q)} \].
The order parameter relaxation time in (3) is given by
\[ \tau_{\eta} (q - Q_c) = \frac{\tau_{\eta} (Q_c)}{1 + (q - Q_c)^2 \xi^2} \].
(4)
where \( \xi \) is the correlation length of the order parameter fluctuations. The last term in (3) quite generally describes

\[ C_{33} (q, \omega) = C_{33}^0 - \frac{a^2 \eta_0^2 (Q_c) \chi_0 (q - Q_c, 0)}{1 - i \omega \tau_{\eta} (q - Q_c) + \frac{\delta^2 i \omega \tau_{th} (q) \chi_0 (q - Q_c, 0)}{1 - i \omega \tau_{th} (q)}} \].
(6)

Equation (6) describes two relaxation processes of a Debye form which are due to fluctuations in the order parameter \( \delta \eta (q - Q_c, t) = \delta \eta (q - Q_c, 0) e^{-i/\tau_{\eta}(q - Q_c)} \) and the temperature \( \delta T (q, t) = \delta T (q, 0) e^{-i/\tau_{th}(q)} \). Since in our measurement geometry (Fig. 1) \( q \) is determined by the thickness of the sample, i.e., \( q = \pi / \lambda = 50 \text{ cm}^{-1} \ll Q_c = \pi / a \approx 10^8 \text{ cm}^{-1} \), the order parameter relaxation time \( \tau_{\eta} \) [Eq. (4)] cannot depend on \( q \). In contrast the thermal relaxation time should strongly depend on the size of the sample, i.e., \( \tau_{th} (q) = (Dq^2)^{-1} = h^2 / D \pi^2 \). Frequency scans with probes of various thicknesses (Fig. 4) yield the quadratic dependence of \( \tau_{th} \) on the sample thickness (Fig. 5). In addition the diffusivity constant determined from this fit is in good agreement with the values for thermal diffusivity constants of molecular crystals. This proves, that the low frequency elastic relaxation which we are probing is due to temperature fluctuations along the \( x \) direction of our sample, i.e., \( \tau_{th} (q) \). As a consequence the second dispersion observed between the 20 Hz and the 10 MHz region (Fig. 2) is due to the order parameter fluctuations [Eq. (6)], i.e., \( \tau_{2} = \tau_{\eta} (Q_c) \ll \tau_{th} (q) \). Using Eqs. (3) and (5) one obtains that the thermal diffusion central peak phenomenon leads to a difference between isothermal and adiabatic elastic response. The isothermal limit \( \omega \tau_{th} \ll 1 \) yields \( \chi_{th}^{-1} = \chi_{\eta K}^{-1} (Q_c, 0) \), the inverse central peak phenomena of various origins. For a heat diffusion central peak \( 1/\gamma \) in (3) is the thermal diffusion time \( \tau_{th} (q) = (Dq^2)^{-1} \),
(5)
where \( D \) is the thermal diffusivity constant. \( \delta^2 = A^2 \eta_0^2 T / C_{\eta} \), where \( C_{\eta} \) is the specific heat at constant \( \eta \). Inserting (3) into (2) one obtains

\[ \tau_{th} (q) = (Dq^2)^{-1} \],
(6)

isothermal susceptibility, whereas for \( \omega \tau_{th} \gg 1 \), \( \omega \tau_{\eta} \ll 1 \) one obtains the adiabatic limit \( \chi_{th}^{-1} = \chi_{\eta K}^{-1} (Q_c, 0) + \delta^2 \). Since \( \tau_{th} \) depends strongly on the \( q \) vector sampled by the experimental technique, the crossover from isothermal to adiabatic behavior occurs at different frequencies depending on the experimental method. For a typical light scattering experiment the momentum transfer \( q = 10^5 \text{ cm}^{-1} \) resulting in \( \tau_{th} (q) = 10^{-7} \text{ s} \) for \( D = 10^{-3} \text{ cm}^2 \text{ s}^{-1} \) [9]. In our case the extremely small wave vector \( q = 50 \text{ cm}^{-1} \) which is given by the thickness \( h \) of the sample yields \( \tau_{th} (q) = 0.12 \text{ s} \) at \( T = 413 \text{ K} \) for \( h = 0.06 \text{ cm} \). Thus for \( f \ll 1 \text{ Hz} \) the isothermal elastic constant is measured (● in Fig. 2) yielding the full elastic anomaly at \( T_c \) [Eq. (6)]. From Fig. 3 it is evident, that the adiabatic elastic constant is measured at frequencies higher than 10 Hz. The large difference between low frequency (20 Hz, □ in Fig. 2) and higher frequency (10 MHz, ■ in Fig. 2) elastic constants is due to a crossover from \( \omega \tau_{\eta} \ll 1 \) to \( \omega \tau_{th} \gg 1 \) region [Eq. (6)], yielding the order parameter relaxation time \( 10^{-3} \ll \tau_{th} \ll 10^{-3} \text{ s} \).

In summary, very slow (1 Hz) elastic relaxations have been found in KSCN below the order-disorder phase transition by low frequency elastic measurements. This

![FIG. 4. Frequency dependences of \( C_{33}^{\text{eff}} \) for various sample thicknesses \( h \) measured at \( T = 413 \text{ K} \). □ \( h = 0.2 \text{ mm} \), ○ \( h = 0.38 \text{ mm} \), △ \( h = 0.5 \text{ mm} \), and ▽ \( h = 0.6 \text{ mm} \).](attachment:image4.png)

![FIG. 5. Thermal diffusion time \( \tau_{th} \) as a function of the thickness \( h \) of the sample, as obtained from the fits of the data of Fig. 4 using Eq. (6). Limits of error are ±3σ values.](attachment:image5.png)
ultralow frequency dispersion is not caused by order parameter fluctuations. To explain our low frequency (0.1–20 Hz) data another relaxation mechanism is required, which we have shown to originate from entropy fluctuations. The physics of this effect is essentially equal to the thermal–diffusion central peak phenomenon observed, e.g., by light scattering in KDP [9]: Because of the $\eta^2 T$ coupling in the free energy (1) the order parameter fluctuations lead to a term $\eta_0(Q_c)\delta \eta(Q_c - q)\delta T(q)$ creating a spectrum of temperature fluctuations $\delta T(q)$ which propagate with characteristic diffusion times $\tau_{\Delta h}(q)$. In a given experiment a particular $q$ component of the temperature fluctuations $\delta T(q)$ is probed. In a scattering experiment $q(=10^5$ cm$^{-1}$) for light scattering is the wave vector transfer to the crystal, whereas in our three-point bending experiment $q(=50$ cm$^{-1}$) is determined by the size $h$ of the sample. This enabled us to verify the sample geometry dependent dispersion $\tau_{\Delta h}(q = \pi/h) \propto h^2/D_{\Delta h}$, which is characteristic for a heat-diffusion central peak mechanism.

To our knowledge this is the first example for the observation of a thermal diffusion central peak in a macroscopic elastic susceptibility.

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