

FIG. 3.4. Types of axial group operation.

$C_n$  = positive rotation through  $2\pi/n$

$\sigma_v$  = reflection across vertical plane (used for family which includes  $xz$  plane).

$\sigma_h$  = reflection across horizontal plane (plane of paper)

$C_2'$  = rotation through  $\pi$  about axis normal to principal axis

$\sigma_d$  = reflection across "dihedral" plane, containing principal axis and bisecting angle between adjacent 2-fold axes (also used in  $C_{4v}$  and  $C_{6v}$  for planes of the family which does *not* include the  $xz$  plane)

$S_n$  = improper positive rotation through  $2\pi/n$  ( $S_n = \sigma_h C_n = i\bar{C}_n$ ). (The bar is used to indicate a *negative* rotation.  $S_2$  is usually denoted by  $i$ .)

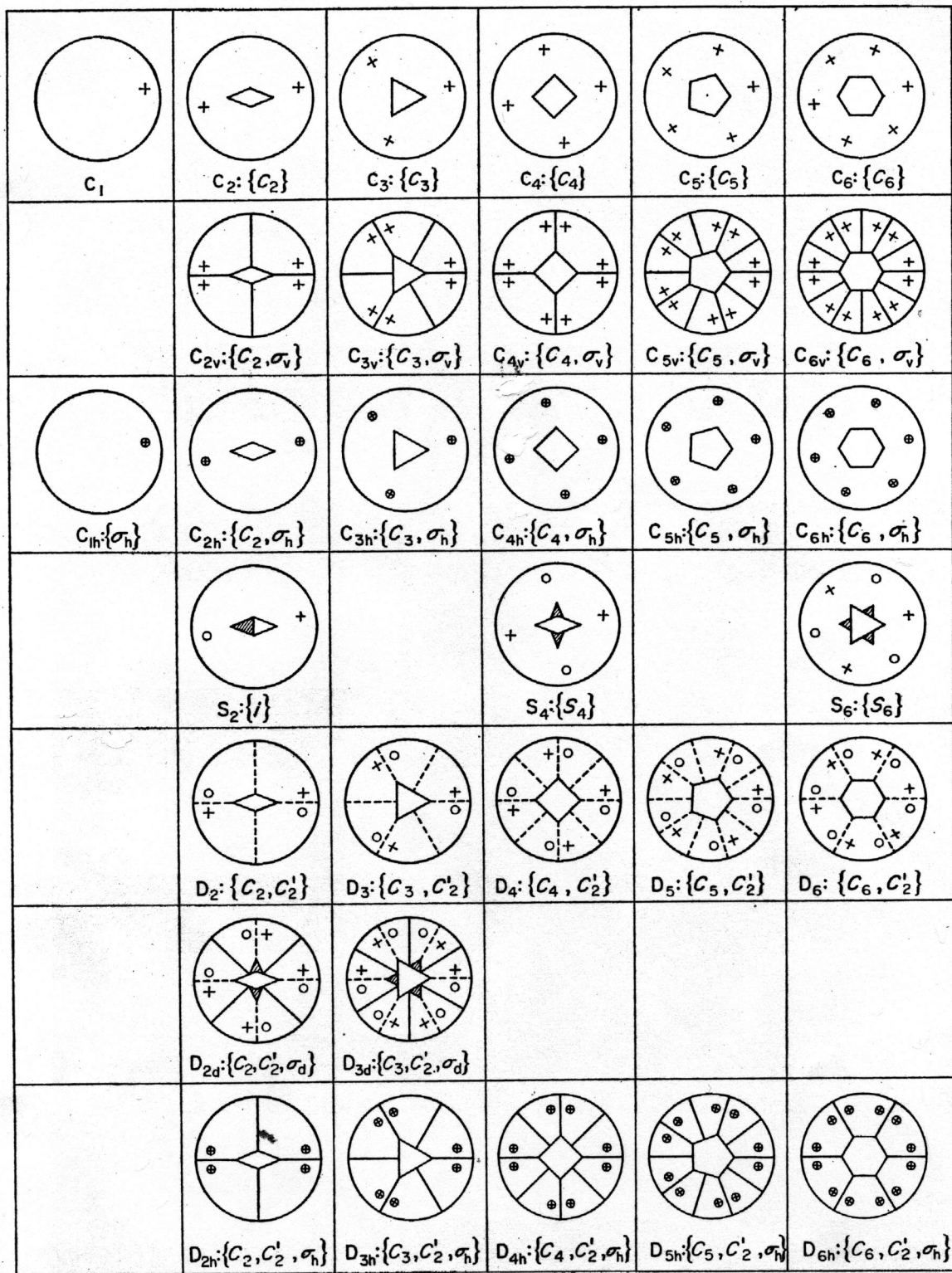


FIG. 3.2. Projection diagrams for axial point groups.

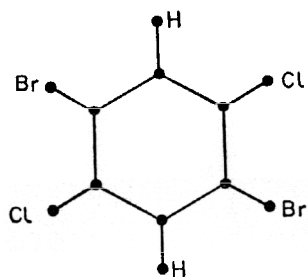
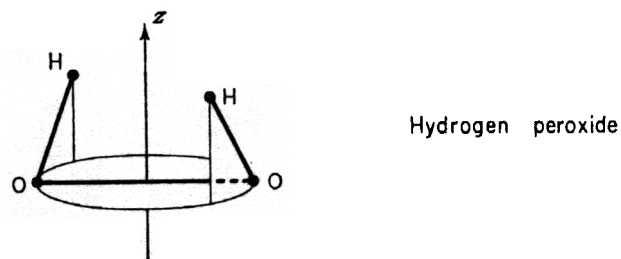


FIG. 3.7. Molecules of symmetry

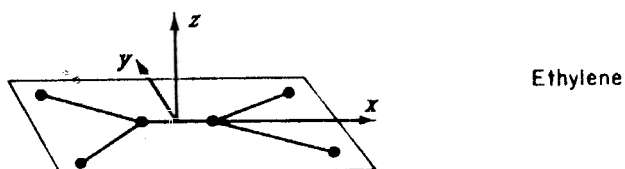
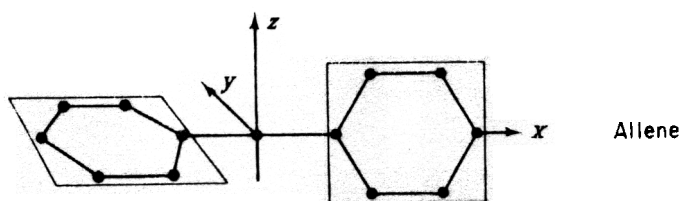
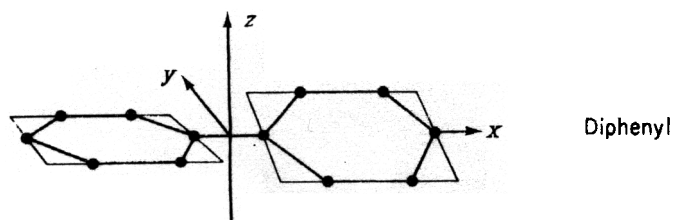


FIG. 3.8. Molecules of symmetry . . . . . In diphenyl the rings are twisted out of plane by steric hindrance between hydrogens (not shown). In allene the rings are perpendicular and the x axis is an improper 4-fold axis.

$D_5$	$E$	$2C_5$	$2C_5^2$	$5C_2$		
$A_1$	1	1	1	1		$x^2 + y^2, z^2$
$A_2$	1	1	1	-1	$z, R_z$	
$E_1$	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	$(x, y)(R_x, R_y)$	$(xz, yz)$
$E_2$	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0		$(x^2 - y^2, xy)$

$D_6$ (622)	$E$	$2C_6$	$2C_3$	$C_2$	$3C_2'$	$3C_2''$		
$A_1$	1	1	1	1	1	1		$x^2 + y^2, z^2$
$A_2$	1	1	1	1	-1	-1	$z, R_z$	
$B_1$	1	-1	1	-1	1	-1		
$B_2$	1	-1	1	-1	-1	1		
$E_1$	2	1	-1	-2	0	0	$(x, y)(R_x, R_y)$	$(xz, yz)$
$E_2$	2	-1	-1	2	0	0		$(x^2 - y^2, xy)$

#### 4. The Groups $C_{nv}$ ( $n = 2, 3, 4, 5, 6$ )

$C_{2v}$ (2mm)	$E$	$C_2$	$\sigma_v(xz)$	$\sigma_v'(yz)$		
$A_1$	1	1	1	1	$z$	$x^2, y^2, z^2$
$A_2$	1	1	-1	-1	$R_z$	$xy$
$B_1$	1	-1	1	-1	$x, R_y$	$xz$
$B_2$	1	-1	-1	1	$y, R_x$	$yz$

$C_{3v}$ (3m)	$E$	$2C_3$	$3\sigma_v$		
$A_1$	1	1	1	$z$	$x^2 + y^2, z^2$
$A_2$	1	1	-1	$R_z$	
$E$	2	-1	0	$(x, y)(R_x, R_y)$	$(x^2 - y^2, xy)(xz, yz)$

$C_{4v}$ (4mm)	$E$	$2C_4$	$C_2$	$2\sigma_v$	$2\sigma_d$		
$A_1$	1	1	1	1	1	$z$	$x^2 + y^2, z^2$
$A_2$	1	1	1	-1	-1	$R_z$	
$B_1$	1	-1	1	1	-1		$x^2 - y^2$
$B_2$	1	-1	1	-1	1		$xy$
$E$	2	0	-2	0	0	$(x, y)(R_x, R_y)$	$(xz, yz)$