Tapered optical fibers (TOFs) with a subwavelength-diameter waist feature a strong evanescent field in the waist region and are widely used to efficiently interface light and matter or to couple light into photonic devices, such as microresonators or photonic crystals. These applications rely on the stability of the phase and polarization of the nanofiber-guided light field and are widely used to efficiently couple light and polarization of the optical mode via the strain-optic effect. Based on an analytic model as well as on experimental measurements, we show that in typical tapered optical fibers these quantities exhibit high-frequency thermal fluctuations. They originate from high-$Q$ torsional oscillations that optomechanically couple to the nanofiber-guided light. We present a simple \textit{ab initio} theoretical model that quantitatively explains the torsional mode spectrum and that can be used to design tapered optical fibers with tailored mechanical properties.

Tapered optical fibers with a nanofiber waist are widely used tools for efficient coupling of light to photonic devices or quantum emitters via the nanofiber’s evanescent field. In order to ensure well-controlled coupling, the phase and polarization of the nanofiber-guided light field have to be stable. Here, we show that in typical tapered optical fibers these quantities exhibit high-frequency thermal fluctuations. They originate from high-$Q$ torsional oscillations that optomechanically couple to the nanofiber-guided light. We present a simple \textit{ab initio} theoretical model that quantitatively explains the torsional mode spectrum and that can be used to design tapered optical fibers with tailored mechanical properties.

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FIG. 1. (Color online) (a) Schematic view of the experimental setup (see text for details). (b) Schematic cross-section profile of the TOF resonator where the radii at the section boundaries and the full opening angles of the conical sections are given. (c) Schematic view of the electrode arrangement used to excite the mechanical modes that consists of two wires that are placed above and below the nanofiber. The latter is oriented perpendicular to the figure.

schematically shown in Fig. 1(b) and consists of a cylindrical nanofiber waist with a radius of \( r_w = 500 \) nm and a length of \( l_w = 10 \) mm which widens in two taper sections on both sides to the initial fiber diameter. Each of the latter is composed of two conical sections with different opening angles which are connected to the waist by a 9-mm-long section with an exponential radius profile where \( \alpha = 0.76 \) mm\(^{-1}\) (see above). After the fabrication process, the fibers are strained by \( \epsilon_w \approx 2\% \) of the nominal waist length and glued to a U-shaped aluminum holder.

The measurement scheme used here detects periodic refractive index variations in the material that are caused by the mechanical vibrations via the strain-optic effect [4,15]. They are observed via polarization fluctuations of the transmitted light or via optical path-length variations using a fiber-integrated optical Fabry-Pérot type cavity [16]. The latter consists of two fiber Bragg grating mirrors (FBGs) with a stop band at a central wavelength of \( \lambda_{FBG} = 852 \) nm and a spectral width of 0.2 nm that are located on both sides of the TOF in the untapered portion of the fiber [see Fig. 1(b)]. We probe the resonator using laser light with a wavelength within the FBG stop band that is launched into the TOF via a fiber coupler [see Fig. 1(a)]. The TOF is placed inside a vacuum chamber with a minimal pressure of \( 10^{-7} \) mbar in order to minimize the mechanical damping from the background gas. At the output port of the fiber, the transmitted light is split by a 50/50 beam splitter and detected with two photodiodes (PD1 and PD2). The signal of PD2 is used to stabilize the frequency of the laser to the side of a Fabry-Pérot fringe at half maximum, thereby maximizing the sensitivity to optical path-length changes and the dynamic range. The stabilization bandwidth of 2 kHz is chosen much smaller than the frequencies of the mechanical modes under study.

For the method in which the polarization fluctuations are detected, we set the laser to a wavelength outside the FBG stop band or, alternatively, use a TOF without a resonator. A polarizing beam splitter cube (PBC) converts the polarization fluctuations to intensity variations that are detected by a photodiode at the PBC’s transmission port. Polarization optics before and after the fiber are used to optimize the signal strength. In addition to passive thermal driving, the mechanical modes can be actively excited by an electric field that exerts an alternating force on stray charges on the insulating silica surface. This field is localized along the nanofiber axis and is generated by two thin and movable electrodes placed above and below the fiber [see Figs. 1(a) and 1(c)].

We first measure the amplitude spectrum of the thermal motion using the polarization method. The resulting spectrum is shown as the lower purple line in Fig. 2. The spectrum features three peaks at frequencies of 162, 321, and 469 kHz, corresponding to three mechanical resonances. These frequencies are approximately integer multiples which indicates that they are harmonics of the same mechanical mode and that the lowest frequency stems from the fundamental mode. We compare this measurement to the spectral response of a TOF with the same radius profile subjected to electric field excitation at a fixed position. For this purpose, a sinusoidal voltage modulation is applied to the electrodes while recording the amplitude at the modulation frequency using a lock-in detection scheme. We obtain a spectral response which shows resonances that coincide with previously observed ones (see the upper blue line in Fig. 2). This confirms the reproducibility of our fabrication method. Additionally, we find resonances with a much smaller frequency spacing in the frequency range beyond 470 kHz. This frequency matches the theoretical cut-off frequency of \( \omega_{co} = 2\pi \times 450 \) kHz for the exponential taper sections. The higher spectral mode density stems from the larger spatial extent of the modes above the cut-off frequency. Furthermore, we observe resonances with a frequency spacing of \( \approx 1.8 \) kHz over the full spectral range (see Fig. 2, inset). By additional finite element method calculations, we confirm that they correspond to transversal modes. In contrast to the torsional modes, transversal modes are not confined by the taper but extend over the full length of the TOF, thereby resulting in the small frequency spacing.

We make an \textit{ab initio} theory prediction for the torsional resonance frequencies that is derived from the design radius...
profile of the TOF and the bulk elastic constants of silica. We omit modes which exhibit a high amplitude near the clamping points and which are therefore expected to suffer from high clamping losses. Such modes stem from the torsional oscillation of the two ends of the TOF which are weakly coupled by the nanofiber. In the simulations, they can be clearly identified via their spatial mode profile and because they come in pairs with a small frequency splitting between the odd and even mode. The predicted frequencies for the remaining modes are marked in Fig. 2 by green disks and show excellent agreement with the observed fundamental and second harmonic torsional resonance frequencies. Furthermore, the theory reproduces the close mode spacing above the cut-off frequency. The precise resonance frequencies in this frequency range are not correctly predicted by the theory. We attribute this fact to deviations between the assumed and the actual radius profile.

We now measure the modal amplitude profiles along the TOF axis for selected modes. This is achieved by recording the response of the TOF to fixed-frequency excitation at different axial positions along the fiber (see Fig. 3). We expect that the effective excitation strength depends on the fiber radius. As a consequence, the measured response is only proportional to the modal amplitude profile in the waist region where the radius is constant. The modal amplitude profiles of the resonances at 162 and 321 kHz resemble that of the first two harmonics of a cylinder with clamped ends. The two higher modes, however, extend much further into the taper region and the mode at \( f = 621.3 \) kHz exhibits nodes in the waist region. Their position and the corresponding uncertainty are indicated by the center and the width of the gray bars in Fig. 3, respectively. We obtain \( \lambda/2 = (6.2 \pm 0.4) \) mm at \( f = (320.6 \pm 4.1) \) kHz, \( \lambda/2 = (3.8 \pm 0.3) \) mm at \( f = (468.9 \pm 1.9) \) kHz, and \( \lambda = (6.0 \pm 0.3) \) mm at \( f = (621.3 \pm 0.2) \) kHz. We compute \( c_t \) using the weighed average of all measurements and obtain

\[
c_t = (3737 \pm 177) \text{ m/s}. \tag{3}
\]

This value is in excellent agreement with the literature value of the torsional acoustic velocity in silica \([3–5]\) (3680 ± 130) m/s and is clearly different from the ones for axial (5630 ± 170) m/s and string modes (1130 ± 35) m/s. This result further substantiates the identification of the mechanical modes as torsional modes of the TOF.

We now measure the \( Q \) factors of the individual mechanical modes using a ring-down technique. We determine the amplitude decay time from an exponential fit which we use to compute the \( Q \) factors listed in Table I. We find high values of \( Q \approx 2.5 \times 10^4 \) for the first two harmonics. The mechanical loss in silica has been studied extensively in literature \([17,18]\). For small structures, such as nanofibers, it is dominated by surface effects which scale with the surface-to-volume ratio (SVR). Based on this model, we obtain a prediction for the nanofiber waist of \( Q = (1.5 \pm 0.5) \times 10^4 \), slightly lower than the measured values. The deviation might be partly due to the fact that the mode extends into the taper region where the SVR is more favorable. Note that the resonance frequencies of the TOF used for this measurement are 9% smaller than for the previous samples. This is due to a lower mechanical strain applied to the sample.

We also study the damping of the torsional modes by the background gas. For this purpose, we measure the \( Q \) factor of the fundamental mode at different gas pressures (see Fig. 4). The \( Q \) factor is approximately constant up to pressures of \( p \sim 10^{-3} \) mbar, meaning that the intrinsic losses dominate, and then decreases due to damping by the background gas. We fit the data by an empirical model that assumes that the damping is proportional to the particle density and find excellent agreement (see the red line in Fig. 4).

Summarizing, we show that tapered optical fibers exhibit optically active mechanical modes. The thermal excitation of these modes at room temperature leads to high-frequency fluctuations of the phase and polarization of the nanofiber-guided light. We measured the spectrum of these fluctuations and found resonances at frequencies of several 100 kHz which we identified as torsional modes. We showed that the widely used exponential radius profile confines these modes to the

<table>
<thead>
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<th>( f ) (kHz)</th>
<th>( 10^4 ) Q</th>
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<tr>
<td>148</td>
<td>2.60 ± 0.05</td>
<td>500</td>
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<td>0.33 ± 0.02</td>
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<td>502</td>
<td>0.71 ± 0.03</td>
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<tr>
<td>401</td>
<td>0.18 ± 0.07</td>
<td>526</td>
<td>0.75 ± 0.03</td>
<td>778</td>
<td>0.31 ± 0.02</td>
</tr>
<tr>
<td>441</td>
<td>1.03 ± 0.03</td>
<td>529</td>
<td>0.11 ± 0.02</td>
<td>817</td>
<td>0.12 ± 0.01</td>
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<td>453</td>
<td>0.17 ± 0.03</td>
<td>545</td>
<td>0.40 ± 0.03</td>
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the measured spectrum and amplitude profiles. It should thus allow one to design the mechanical spectrum according to experimental needs.

Our findings have important consequences for the use of tapered optical fibers in a high vacuum environment. As an example, first estimations show that the thermal polarization fluctuations found in this work currently limit the storage time of nanofiber-based atom traps [9,10]. They might also limit the ultimate ideality of fiber coupling to photonic devices [19]. More generally, high-$Q$ torsional resonances may also occur in other kinds of freestanding subwavelength-diameter waveguides and may influence the stability of the guided light fields. This applies, in particular, to the case of polarization maintaining structures where the torsional vibration directly translates into the polarization rotation.

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